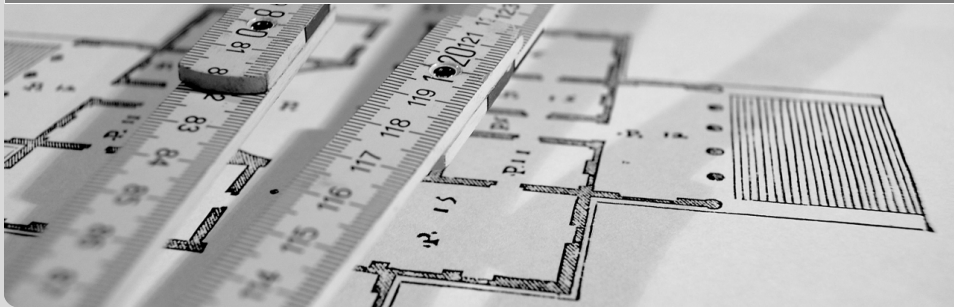


A Comparative Study of Incremental Constraint Solving Approaches in Symbolic Execution

Presentation at HVC2014, Haifa.

Tianhai Liu¹, Mateus Araújo², Marcelo d'Amorim², and Mana Taghdiri¹ | November 18, 2014

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Symbolic Execution

- introduced 40 years ago.
- automatically generate high-coverage tests for complex software.
- popular and practical in recent years.
- various tools exist, e.g., KLEE, SPF, PEX.

Bottlenecks

- space cost: space exploration in path exploration.
- time cost: constraint solving in the solver.

We focus on reducing the **time cost**.

Introduction by an Example

Code

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2     int b,int c){  
3     int res = 0;  
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9 }  
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11     x,y,z:=sym_input();  
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13     assert(w>=x);  
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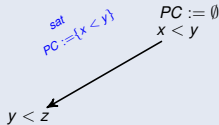
Symbolic Execution Tree

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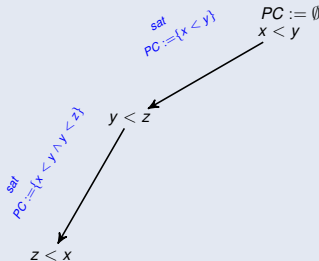


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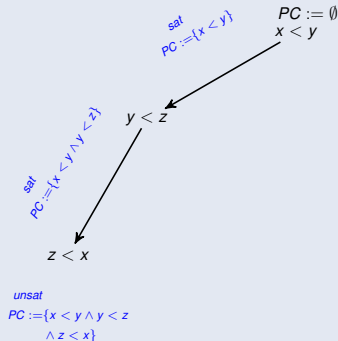


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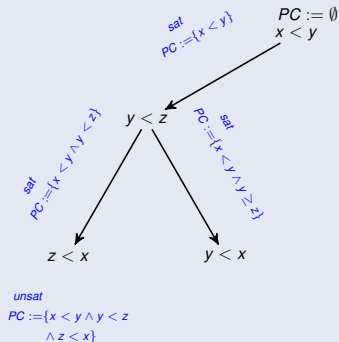


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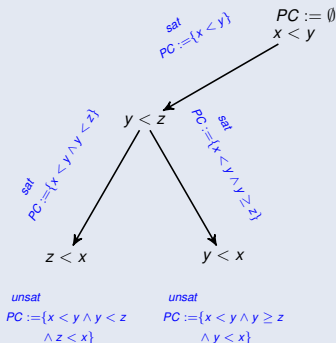


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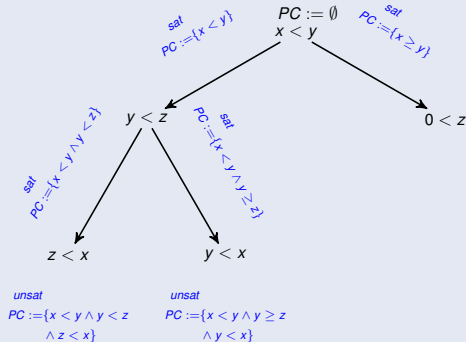


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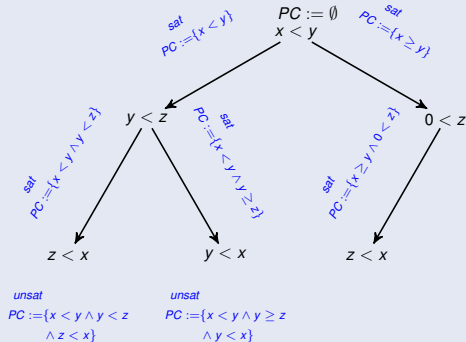


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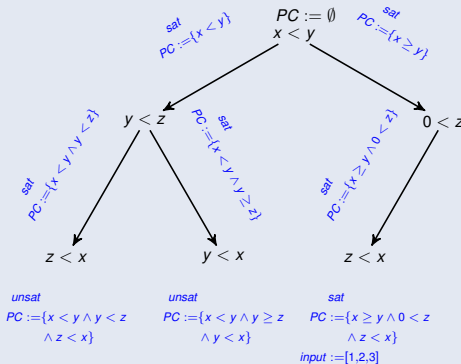
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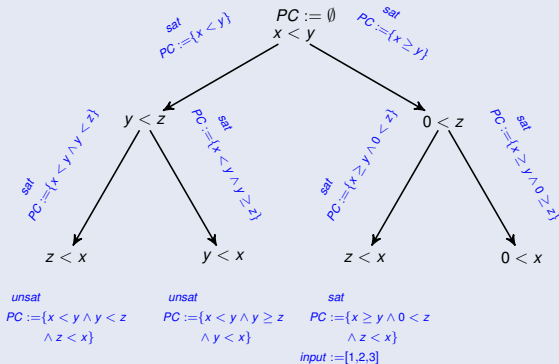


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Symbolic Execution Tree



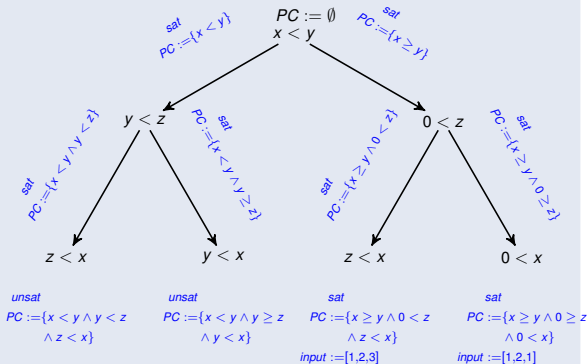
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Symbolic Execution Tree



caching: reuse solutions of solved constraints.

- simplify new constraints with independent clauses optimization.
- introduce cost of partitioning constraints and operating cache.
- popular used in tools, e.g., KLEE, SPF, PEX

cachingOpt: same to *caching* but building partitions incrementally.

- build new partition by combining new constraint with dependent partitions.
- introduce overhead in combination.

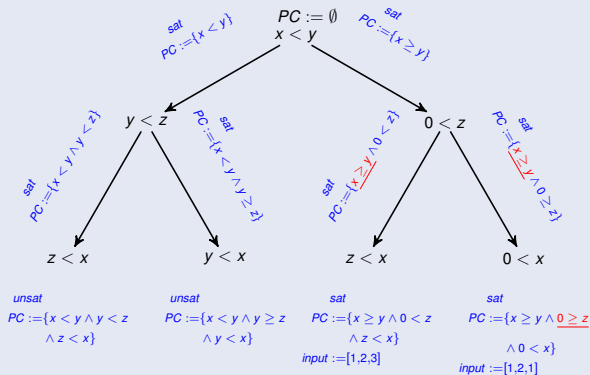
Code

Symbolic Execution Tree

```

1 int biggest(...){
2   int res = 0;
3   if (a < b)
4     res = b;
5   if (res < c)
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8 }
9 ...

```



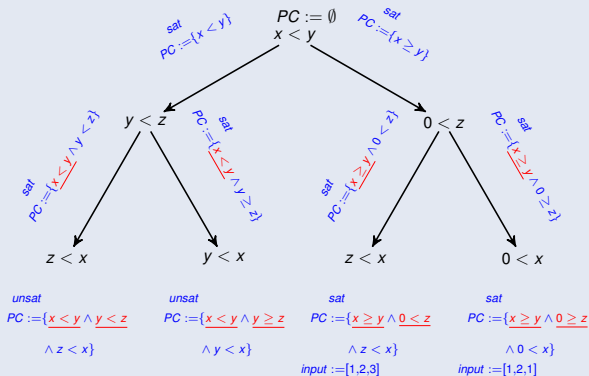
stack

- use incremental SMT solving.
- create new frame on the assertion stack of the solver for each query.
- build new path-conditions in path exploration.

```

1 int biggest(...){
2   int res = 0;
3   if (a < b)
4     res = b;
5   if (res < c)
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7   return res;
8 }
9 ...

```



Optimization: *stackOpt*

- same to *stack* but with common sub-expression elimination(CSE).
- find shared expressions outside of constraint solvers.
- introduce new variables referring to shared expressions.

Research Questions

- How cache-based and stack-based approaches compare?
- What is the benefit of using common sub-expressions elimination?
- Where each technique spends most time?

Benchmarks

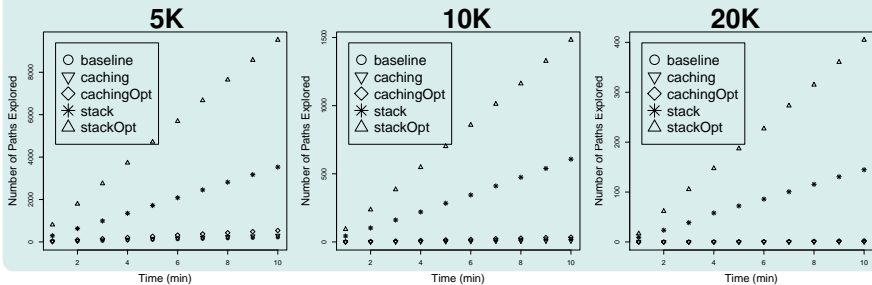
- **RUGRAT**: 300 programs of 5, 10, 20 KLOC, 100 programs for each program size. (~4300 KLOC together).
- **KLEE**: 96 Unix programs, e.g., cat, sed. (~4.5 KLOC together)

Environment

- Intel CPU with 2.60 GHz running 64-bit openSUSE
- 8GB max heap size for each running

RQ1: Cache* VS Stack* on RUGRAT

Number of paths explored in 10min



Observations

- incremental SMT solving is beneficial.
- fewer paths are generated when exploring longer programs.
- linear x-y relationship in the average plots.

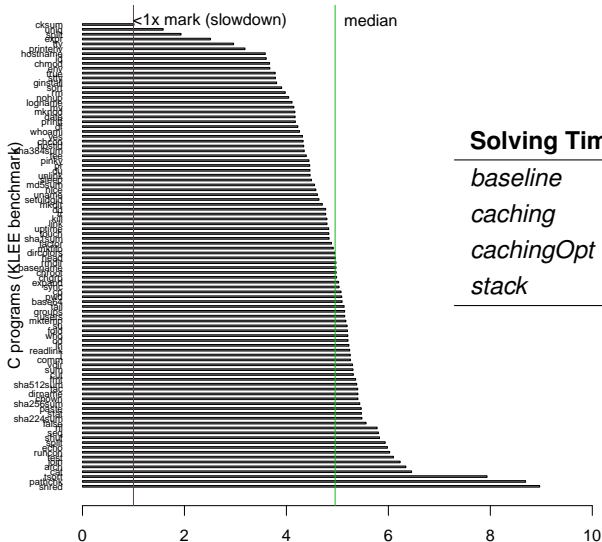
Constraint Generation of KLEE

- use KLEE's default configuration^a
- run KLEE on 96 programs from KLEE Coreutils benchmark (total 101 programs).
- KLEE spent $\sim 27s$ (90% = $27s/30s$) in constraint solving.
- *stack* spends average 7.53s. (best case 0.14s, worst case 72.36s, median 6.3s)
- all 91/96 programs had been solved under 10s.

^a<http://klee.github.io/klee/klee-tools.html#klee-stats>

RQ1: Cache* VS Stack* on KLEE

Speedup (x times quicker than best other)

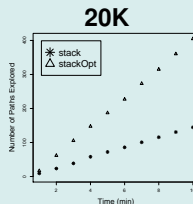
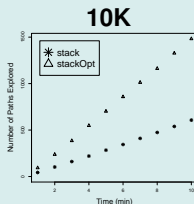
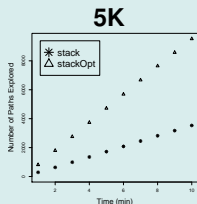


Solving Time (ms) per query

<i>baseline</i>	34.559
<i>caching</i>	26.231
<i>cachingOpt</i>	25.860
<i>stack</i>	7.260

RQ2: Effects of Common Sub-expression Elimination

Number of paths explored for RUGRAT benchmark in 10min



Discussion

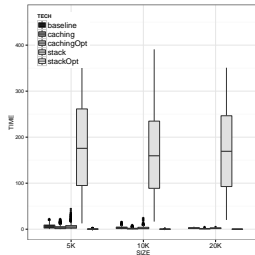
- *stackOpt* reuses the constraints built before path exploration, while *stack* constructs new constraint on each node.
- SMT solver finds shared expressions at SMT formulas (syntactical) level, while *stackOpt* finds them at Java (semantic) level.

Runtime Cost

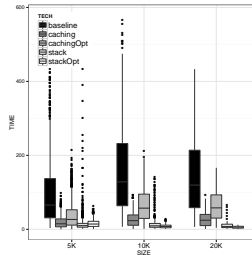
- *path exploration*: exploring paths.
- *expression construction*: creating Z3 internal expressions.
- *constraint solving*: solving and caching constraints.
- *rest*: others, e.g. code transformation.

RQ3: Time-breakdown

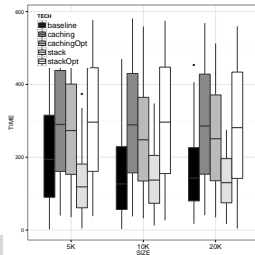
Path Exploration



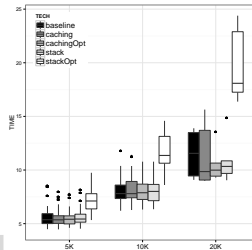
Expression Construction



Constraint Solving



Rest



Implementation

- use Soot to parse Java source/binary code.
- use Jung to construct symbolic execution tree.
- use InspectJ to unroll loops and inline methods.
- use Z3 API to solve constraints.

Caching schemes

- Cadar *et al.* proposed several optimizations to simplify constraints prior to invoking the solver in KLEE. In addition, KLEE checks constraints with a potential solution.
- Visser *et al.* proposed GREEN to share results of symbolic executions across different environments. Our contributions are complementary to GREEN to speedup constraint solving.

Incremental SMT solving

- Incremental SMT solving is used in some situations. e.g., solving scheduling problems.
- Wieringa proposed a technique to enhance the clause learning by executing the solver in multiple threads.

Conclusion

- Incremental constraint solving is important in SE.
- Stack-based approaches provides superior results compared to cache-based approaches in our experiments.

Challenges

- Integrate syntactic and semantic approaches. E.g., how to get semantic information from SMT solvers?
- Handle the theories not supported in SMT solvers efficiently. E.g., how to represent floating-point numbers in SMT solvers?

Reproduce Experiments

http://asa.iti.kit.edu/130_392.php